## Worksheet \#23

(1) Find the equation of the tangent plane to the surface $z=2 e^{3 y} \cos (2 x)$ at $(\pi / 3,0,-1)$.
(2) Find all points on the surface $z=x^{2}-2 x y-y^{2}-8 x+4 y$, where the tangent plane is horizontal.
(3) Use the total differential $d z$ to approximate the change in $z$ as $(x, y)$ moves from $P$ to $Q$ where $z=\ln \left(x^{2} y\right)$ where $P(-2,4)$ and $Q(-1.98,3.96)$.
(4) In determining the specific gravity of an object, its weight in air is found to be $A=36 \mathrm{lbs}$ and its weight in water is $W=20 \mathrm{lbs}$, with a possible error in each measurement of 0.02 lb. Approximate the error in calculating the specific gravity $S$, where $S=A /(A-W)$.

