

**Group Work Tip #4.** After the discussions had in class in relation with a handout, it is everybody's duty to carefully write down solutions to all the problems. This is a thing that I *expect* everybody to do.

**Exercise 14.6.** Every monotone function on  $[a, b]$  is Riemann integrable.

**Exercise 14.7.** If  $f : [a, b] \rightarrow \mathbb{R}$  is integrable and  $|f(x)| \leq M$ , for all  $x \in [a, b]$ , then

$$\left| \int_a^b f(t) dt \right| \leq M(b - a).$$

**Exercise 14.8.** An **antiderivative** of  $f$  is a continuous function  $F$  such that  $F'(x) = f(x)$ , for all  $x$  in the domain of  $f$ . Show that every continuous function on  $f : [a, b] \rightarrow \mathbb{R}$  has an antiderivative. Moreover, if  $G$  is any antiderivative of  $f$ , then:

$$\int_a^b f(t) dt = G(b) - G(a).$$