| INSTRUMENT | COMMENTS | MODES <br> (fundamental $\mathrm{f}_{1}$ and partials) |
| :---: | :---: | :---: |
| STRINGS | String held under tension at two ends: $f_{l}=v / 2 L$, where $v=(T / m)^{1 / 2}$ is velocity of wave on string | $\mathrm{f}_{1}, 2 \mathrm{f}_{1}, 3 \mathrm{f}_{1}, 4 \mathrm{f}_{1}, \ldots$ (harmonic) |
| Acoustic Guitar | Plucked strings; bridge couples string vibration to sounding board | $\mathrm{f}_{1}, 2 \mathrm{f}_{1}, 3 \mathrm{f}_{1}, 4 \mathrm{f}_{1}, \ldots$ (harmonic) |
| Electric Guitar | Plucked strings; electromagnetic transducer couples string vibration to an electronic signal | $\mathrm{f}_{1}, 2 \mathrm{f}_{1}, 3 \mathrm{f}_{1}, 4 \mathrm{f}_{1}, \ldots$ (harmonic) |
| Harsichord | Plucked keyboard instrument; can't vary loudness | $\mathrm{f}_{1}, 2 \mathrm{f}_{1}, 3 \mathrm{f}_{1}, 4 \mathrm{f}_{1}, \ldots$ (harmonic) |
| Piano | Complex key action allows variation of loudness | $\mathrm{f}_{1}, 2 \mathrm{f}_{1}, 3 \mathrm{f}_{1}, 4 \mathrm{f}_{1}, \ldots$ (harmonic) |
| Violin, Cello, etc. | Intricate sound board couples all frequencies well. Bowing action gives rapid stick/slip oscillation | $\mathrm{f}_{1}, 2 \mathrm{f}_{1}, 3 \mathrm{f}_{1}, 4 \mathrm{f}_{1}, \ldots$ (harmonic) |
| WINDS | Tubular air resonator with finger holes first open hole from top determines effective length L ). One or more "register holes" near mouthpiece produce an octave or more higher when opened. |  |
| Organ pipes (no finger or register holes) | Open/open or open/closed nearly cylinderical pipes. Source coupling: air blown around obstacle open ended: $f_{l}=v / 2 L$ ( $\mathrm{v}=$ velocity of sound). closed ended: $f_{l}=v / 4 L$ | open: $\mathrm{f}_{1}, 2 \mathrm{f}_{1}, 3 \mathrm{f}_{1}, 4 \mathrm{f}_{1}, \ldots$ (harmonic) <br> closed: $\mathrm{f}_{1}, 3 \mathrm{f}_{1}, 5 \mathrm{f}_{1}, 7 \mathrm{f}_{1}, \ldots$ (odds only) |
| Recorder | Open/open ended cylindrical pipe, $f_{I}=v / 2 L$ Source coupling: air blown around obstacle | $\mathrm{f}_{1}, 2 \mathrm{f}_{1}, 3 \mathrm{f}_{1}, 4 \mathrm{f}_{1}, \ldots$ (harmonic) |
| Flute (transverse) | Open/open ended cylindrical pipe , $f_{l}=v / 2 L$ <br> Source coupling: air blown across transverse hole at top | $\mathrm{f}_{1}, 2 \mathrm{f}_{1}, 3 \mathrm{f}_{1}, 4 \mathrm{f}_{1}, \ldots$ (harmonic) |
| Clarinet | Closed/open ended pipe with finger holes, $f_{l}=v / 4 L$ Source coupling: single reed vibrates against mouthpiece | $\mathrm{f}_{1}, 3 \mathrm{f}_{1}, 5 \mathrm{f}_{1}, 7 \mathrm{f}_{1}, \ldots$ (odds only) |
| Oboe, Bassoon, English Horn | Conical pipe [like open/open pipe!], $f_{l}=v / 2 L$ <br> Source coupling: double reed vibrates against eachother | $\mathrm{f}_{1}, 2 \mathrm{f}_{1}, 3 \mathrm{f}_{1}, 4 \mathrm{f}_{1}, \ldots$ (harmonic) |
| Saxophone | Conical pipe [like open/open pipe!], $f_{l}=v / 2 L$ <br> Source coupling: single reed vibrates against mouthpiece | $\mathrm{f}_{1}, 2 \mathrm{f}_{1}, 3 \mathrm{f}_{1}, 4 \mathrm{f}_{1}, \ldots$ (harmonic) |
| BRASS |  |  |
| Trumpet, French Horn, Euphonium (baritone), Tuba | Closed/open coiled tubing. Mouthpiece at input and tapered bell at output strongly influence modes. Three valves change tubing length; overblowing mouthpiece allows higher partials Source coupling: lips vibrate inside mouthpiece Pedal tone: rough vibration at $\mathrm{f}_{1} / 2$ (octave below fundamental) | $\begin{aligned} & \hline \mathrm{f}_{1}, 1.5 \mathrm{f}_{1}, 2 \mathrm{f}_{1}, 2.5 \mathrm{f}_{1}, \ldots \\ & \text { (plus pedal tone at } 0.5 \mathrm{f}_{1} \text { ) } \end{aligned}$ |
| Trombone | Same as trumpet family, with continuous sliding tube length instead of valves | $\begin{aligned} & \hline \mathrm{f}_{1}, 1.5 \mathrm{f}_{1}, 2 \mathrm{f}_{1}, 2.5 \mathrm{f}_{1}, \ldots \\ & \text { (plus pedal tone at } 0.5 \mathrm{f}_{\mathrm{l}} \text { ) } \end{aligned}$ |
| PERCUSSION | Usually a complex mode spectrum, and often not pitched (noisy) |  |
| Unpitched percussion: snare drum, bass drum | Two-dimensional modes complicated and not usually harmonic. no pitch here, but a contribution from a near continuum of frequencies |  |
| Cymbals, tam-tam | Metallic disks (usually bronze) producing noisy splashing sound, no definite pitch |  |
| Gong | Metallic disks (usually bronze) producing splashing sound with definite fundamental pitch |  |
| Pitched drums: Timpani (or Kettle) Drums | Lowest frequency mode dies fast and is percussive and dissonant; next several modes are near harmonics, carefully engineered by shape of kettle bowl beneath drum head | $\mathrm{f}_{1}, 1.5 \mathrm{f}_{1}, 2 \mathrm{f}_{1}, 2.5 \mathrm{f}_{1}, 3 \mathrm{f}_{1}, \ldots$ |
| Marimba | Rosewood bars suspended and shaved so that first partial is at $4 \mathrm{f}_{1}$. Resonator underneath has fundamental mode air mode at $f_{1}$ | $\mathrm{f}_{1}, 4 \mathrm{f}_{1}, \ldots$ |
| Xylophone | Rosewood bars suspended and shaved so that first partial is at $3 \mathrm{f}_{1}$. Resonator underneath has fundamental mode air mode at $\mathrm{f}_{1}$ | $\mathrm{f}_{1}, 3 \mathrm{f}_{1}, \ldots$ |
| Vibraphone, Glockenspiel | Metal bars suspended and shaved so that first partial is at $4 f_{1}$. Resonator underneath has fundamental mode air mode at $\mathrm{f}_{1}$. Oscillating dampers above resonator produces tremolo in volume. | $\mathrm{f}_{1}, 4 \mathrm{f}_{1}, \ldots$ |
| Tubular Bells (Chimes) | Nearly harmonic series of partials, but fundamental is absent. We hear fundamental anyways!!! | $\begin{aligned} & \left(\mathrm{f}_{1} \text { heard but absent }\right), 2 \mathrm{f}_{1}, 3 \mathrm{f}_{1} \text {, } \\ & 4 \mathrm{f}_{1}, \ldots \text { (harmonic) } \end{aligned}$ |
| Carillon Bells | Bell shape produces a minor triad and a major triad one octave higher. Plus "buzz tone" one octave below $\mathrm{f}_{1}$ fundamental | $\mathrm{f}_{\mathrm{l}}, 1.2 \mathrm{f}_{\mathrm{l}}, 1.5 \mathrm{f}_{1}, 2 \mathrm{f}_{1}, 2.5 \mathrm{f}_{\mathrm{l}}, 3 \mathrm{f}_{1}, 4 \mathrm{f}_{1}, \ldots$ |

