## Worksheet \#3: Counting periodic orbits

Consider the logistic function $G(x)=4 x(1-x)$. Plot $G^{2}(x), G^{3}(x)$ and $G^{4}(x)$.




(1) How many fixed points of $G^{3}$ should there be?
(2) How many fixed points of $G^{3}$ are in 1-period orbits? 2-period orbits? [Hint: which lower periods give fixed points of $G^{3}$ ?]
(3) So how many period 3 orbits are there?
(4) How many fixed points of $G^{k}$ are there?

Complete the periodic table.

| period-k | \# of fixed points of $G^{k}$ | \# of fixed pts due to lower periods | \# of k -periodic orbits |
| :---: | :---: | :---: | :---: |
| 1 | 2 | 0 | 2 |
| 2 | 4 | 2 | 1 |
| 3 |  |  |  |
| 4 |  |  |  |
| 5 |  |  |  |
| 6 |  |  |  |
| 7 |  |  |  |

