## Worksheet #3: Counting periodic orbits

Consider the logistic function G(x) = 4x(1-x). Plot  $G^2(x)$ ,  $G^3(x)$  and  $G^4(x)$ .



(1) How many fixed points of  $G^3$  should there be?

- (2) How many fixed points of  $G^3$  are in 1-period orbits? 2-period orbits? [Hint: which lower periods give fixed points of  $G^3$ ?]
- (3) So how many period 3 orbits are there?
- (4) How many fixed points of  $G^k$  are there?

Complete the periodic table.

period-k	# of fixed points of $G^k$	# of fixed pts due to lower periods	# of $k$ -periodic orbits
1	2	0	2
2	4	2	1
3			
4			
5			
6			
7			