

Hints for HW6

You will need to read (4.29) to (4.34) (p. 236-7 of book). That's it.

Once you have solved the c_j coeffs, (4.31) can give you $u(x)$, as in (4.34)

The ^{"spectrum"} eigenvalues of K is same as those of A matrix.

The eigenfunc. of K is then $\sum c_j \vec{x}_j(x)$ where \vec{x}_j is the eigenvec. of A .

All for my question A)... just work through as in Example 4.15

(Don't need any of §4.3.4).

- #13 a Hint: $\int_0^{1/2} u(y) dy$ is constant (as a func of x). Call it c .
Now integrate the whole eqn, solve for $u(x)$. You don't need anything from §4.3.3-4.
- b. Think in the same way.
- c. Apply $n=1$ case of Example 4.15

- #14. Nothing from book needed. Hint: what functional form in x must $Ku(x)$ take, regardless of form of u ? So is there an eigenfunction (what if you put this in as u ?) What is eigenvalue?

Remember

$$Ku = \lambda u$$

defines eigenfunction & eigenvalues.

- #4. — all parts of #4 use same ideas you learned for Volterra, i.e. trying to turn it into an ODE IVP by repeated differentiation. Nothing new here.
- b: Use $\int_0^1 \min(x,y) u(y) dy$
 $= \int_0^x y u(y) dy + x \int_x^1 u(y) dy$
- Set $\lambda u = Ku$ then differentiate twice, via Leibniz formula.
- c: Use same ideas as b. a: $\lambda u = Ku$ use Fourier series & the hint.
- d: This is actually a one-word answer ... we did it in today's lecture.