

Instructions: This is a 20-minute quiz consisting of short answer questions. Give enough justification so that I can tell what you were thinking if you make a mistake. The quiz is worth 50 points.

1. Consider the following preference system:

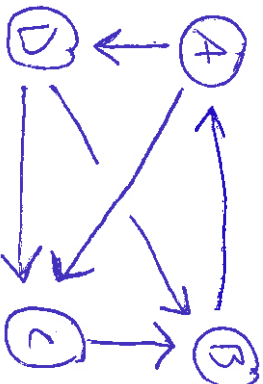
6	5	3	7
A	B	B	C
B	A	C	A
C	C	A	B

- (a) Who is the plurality winner? B - 8 votes
- (b) Is there a Condorcet winner? Yes If so, who? A
- (c) Who is the Borda winner? A

2. Consider the following preference system:

9	2	4	6
A	B	D	C
D	A	C	B
C	D	B	D
B	C	A	A

(a) Draw the preference graph for these votes:



(b) What ordering of sequential votes allows option C to win? A D B C or D A B C

First comparison: A → D Second comparison: B → A Third comparison: C → B

(c) Select (non-negative) Borda weights so that option D is the winner:

First place: 10 Second place: 9 Third place: 1 Fourth place: 0

Lots of possible choices here!

3. Use IESDS on the following matrix to determine the possible equilibria:

2,1	3,0	5,-3	7,-5
-4,7	-5,0	6,-4	1,6
-5,-1	0,5	2,-5	-1,-3
-4,5	0,-3	-1,-4	7,-5

For Player 2 the third & fourth columns are dominated by column 1.

Then, for Player 1 the top column dominates all the lower ones,

Finally, for Player 2 (3,0) is preferable to (2,-1)

4. Find the Nash equilibria for the following game:

0,0	1,1	2,2	4,4
-3,2	-1,4	5,1	3,3
1,3	8,22	2,5	1,1
4,4	6,40	3,1	-1,-1

(1,1) (8,22)

5. When we discussed the game of **Chicken** in class, we noted that "choosing" to go first by announcing your intention could improve your expected outcome in the game. Circle the game below in which player 1 would like to play first. Why?

5,-5	3,4
3,2	-1,5

2,4	-1,-3
-5,0	4,6

In the top game there is a unique Nash equilibrium (3,4), so the first player doesn't improve their outcome by playing first. On the other hand, the lower game has two Nash equilibria and Player 1 can get the better outcome of (4,6) by announcing that they will play the bottom row.