

3. List some interesting things you notice. Are there relationships between the center and various centralizers? Is one always contained in the other? Is every element of G always in some centralizer.

4. Carefully read through the proof that $Z(G) \leq G$ on page 65. Now prove for each a in a group G , the centralizer of a is a subgroup of G .

5. Let G be a group, and let $a \in G$. Prove that $C(a) = C(a^{-1})$.

6. Let G be a group and consider the set $\bigcap_{a \in G} C(a)$. Use your calculations in Problem 2, to find $\bigcap_{a \in D_4} C(a)$. Is this what you expected? Use this information to conjecture a theorem. Prove your theorem.