Math 23 Diff Eq: Homework 1

due Wed Sept 28 ... but best if do relevant questions after each lecture

Some of your homework time this week is devoted to getting started with Matlab, a versatile and powerful package which I promise will bring you joy and success in your future careers! For help, always start with our course website http://math.dartmouth.edu/~m23f05, then ask friends or myself.

A. Install Matlab on your personal machine, e.g. from http://hydra.dartmouth.edu/matlab/downloads.

Susan Schwarz can help with installation. Instead you could work at computer labs where Matlab is already installed. Try out a couple of commands from the Matlab introductions linked on our course site (don't worry about matrices yet). Try t=-2:.01:2; y=exp(t); plot(t,y);

B. Exploring direction fields and solution families.

Download dfield7 to your desktop or working directory and run it from Matlab. (Failing that, use the Java version).

Use it to plot the direction field superposed on some solutions to y' = 3 - y with different initial conditions $y(0) = y_0$. Hand in printout of this.

i) Describe in words the relationship between the direction field and a solution passing through a given point (t, y).

ii) Describe the behavior as $t \to \infty$ (unstable, growth/decay, etc). Does it depend on y_0 ?

Problems from Boyce & DiPrima: (remember to show your working/reasoning—answers without explanation will not receive a high score!)

- **1.1**: 2, 20 (don't use computer), 22.
- **1.2**: 7, 12.
- **1.3**: 1, 9, 16.
- **2.1**: 1 [Hint: in dfield7 you will want to enter y' = -3*t + t + exp(-2*t)], 15, 20.
- **2.2**: 2, 6 (look for constant solutions too), 21 (convert the y values where y' goes undefined to x values. Finally use dfield7 to visualize intergral curve—you may need to Stop the solver yourself for each curve).
- **2.4**: 1 (linear or nonlinear?), 8 (easy).