

# Modeling New Hampshire ISO-NE 24-Hour Real-Time Power Prices Based on Seasonal Data

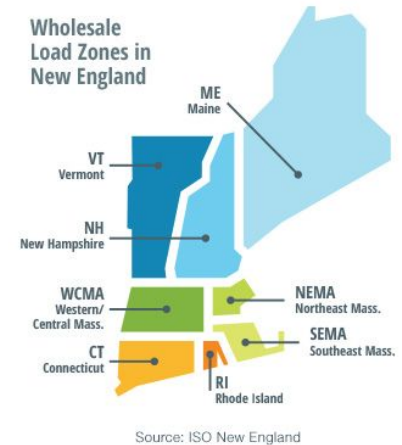
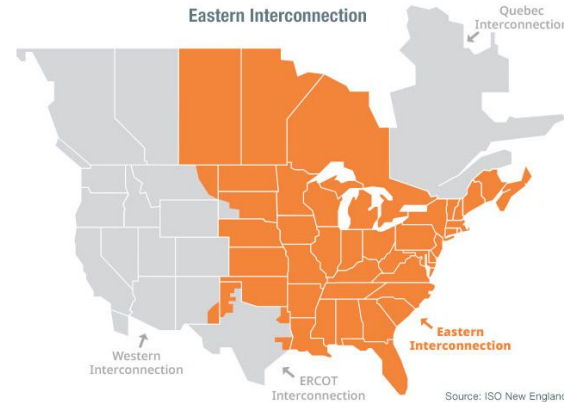
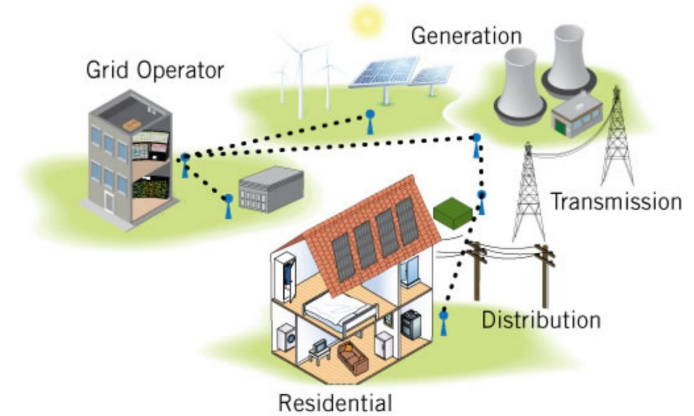
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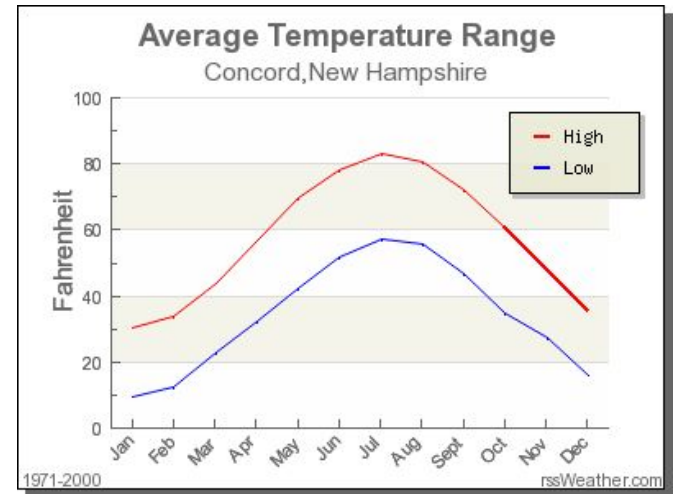
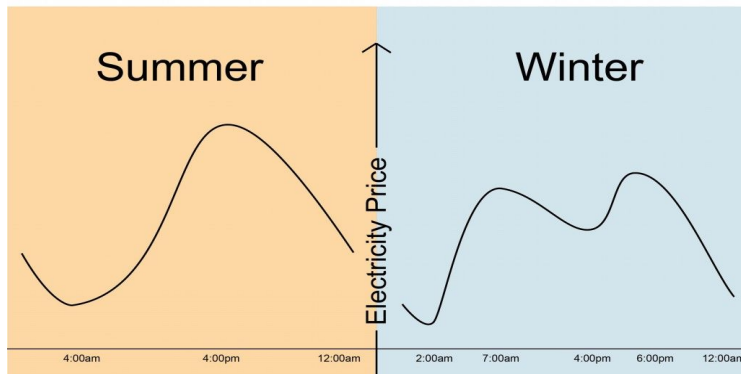
# Background

- Power prices are for electricity market
- 3 main zones in United States
- New Hampshire market is partly regulated
  - We focus on regulated ISO-NE Market
- Data used prices on a 24-hour Real-Time Basis
  - Average prices throughout day
  - Prices based on Real-Time Usage



# Expectations in Pricing Trends

- Summer and winter will be highest
  - Heating usage during cold New Hampshire winters
  - A/C usage during hot New Hampshire summers
- Outliers exist especially during holidays
- General daily trends involve:
  - Extensive usage during morning and late-afternoon



# Graph Approximation Equation

$$Y = A + B*\sin(x) + C*\cos(x) + D*\sin(2x) + E*\cos(2x)$$

# MATLAB Code

<code>y = [48.89, ... , 21.76];</code>	→	Lists 146 energy prices corresponding to each week after Jan 1st 2017
<code>x = [1:146]';</code>	→	x from 1 to 146 (representing each week starting Jan 01 2017)
<code>x1 = sin ((2*pi/52)*x);</code>	→	[sin(x)]
<code>x2 = cos ((2*pi/52)*x);</code>	→	[cos(x)]
<code>x3 = sin ((4*pi/52)*x);</code>	→	[sin(2x)]
<code>x4 = cos ((4*pi/52)*x);</code>	→	[cos(2x)]
<code>x5 = ones (146,1);</code>	→	[column of ones for constant]

→ *As the prices cycle every 52 weeks (annually) the inside of sine & cosine must be  $x/52$  so the curve fit matches this annual cycle.*

## MATLAB Code

- `X = [x1, x2, x3, x4, x5];` → Create new variable, X, containing 1, sin(x), cos(x), sin(2x), cos(2x)
- `coefficients = (X'*X)\(X'*y)` → Matrix division to find coefficients (A,B,C,D,E)
- `graph = X * coefficients;` → graph corresponds to the y values of the approximation graph
- `plot (x, graph, 'linewidth', 1.5)` → Plots x values (0-146) against the graph to produce the sin/cosine curve fit
- `hold on` → *Graph function (not important)*
- `scatter (x,y)` → Plots the actual values from the data

# MATLAB Code + Results

```
xlabel('Weeks starting Jan 2017');
```

→

Labelling the graph

```
ylabel('Energy price');
```

→

Labelling the graph

Coefficients we got from the equation were:

A = 36.5435

B = -0.1416

C = 14.9648

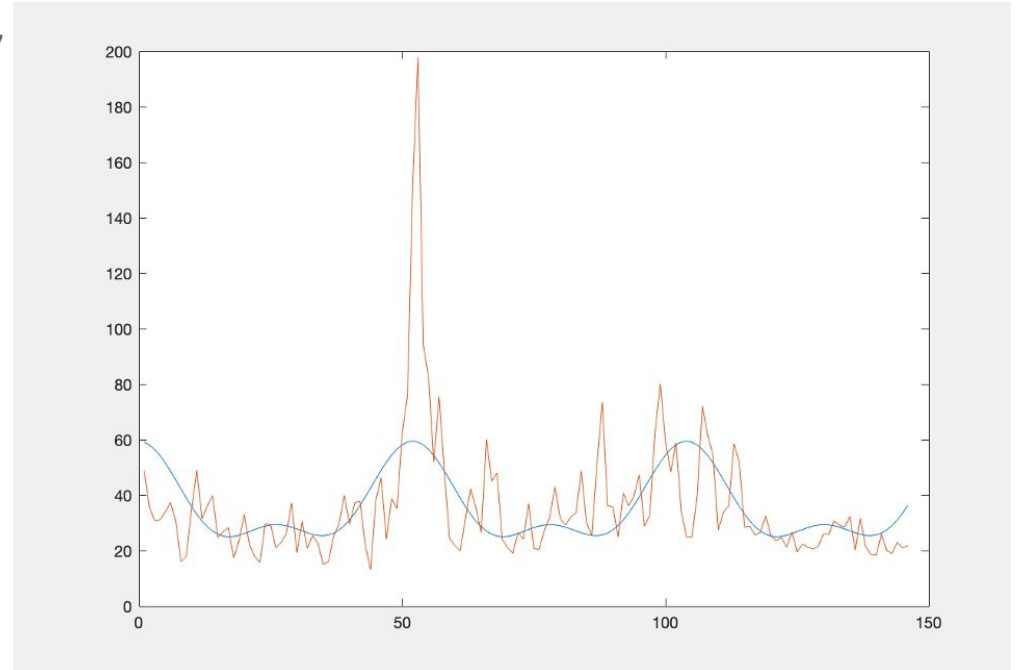
D = 1.1266

F = 7.7712

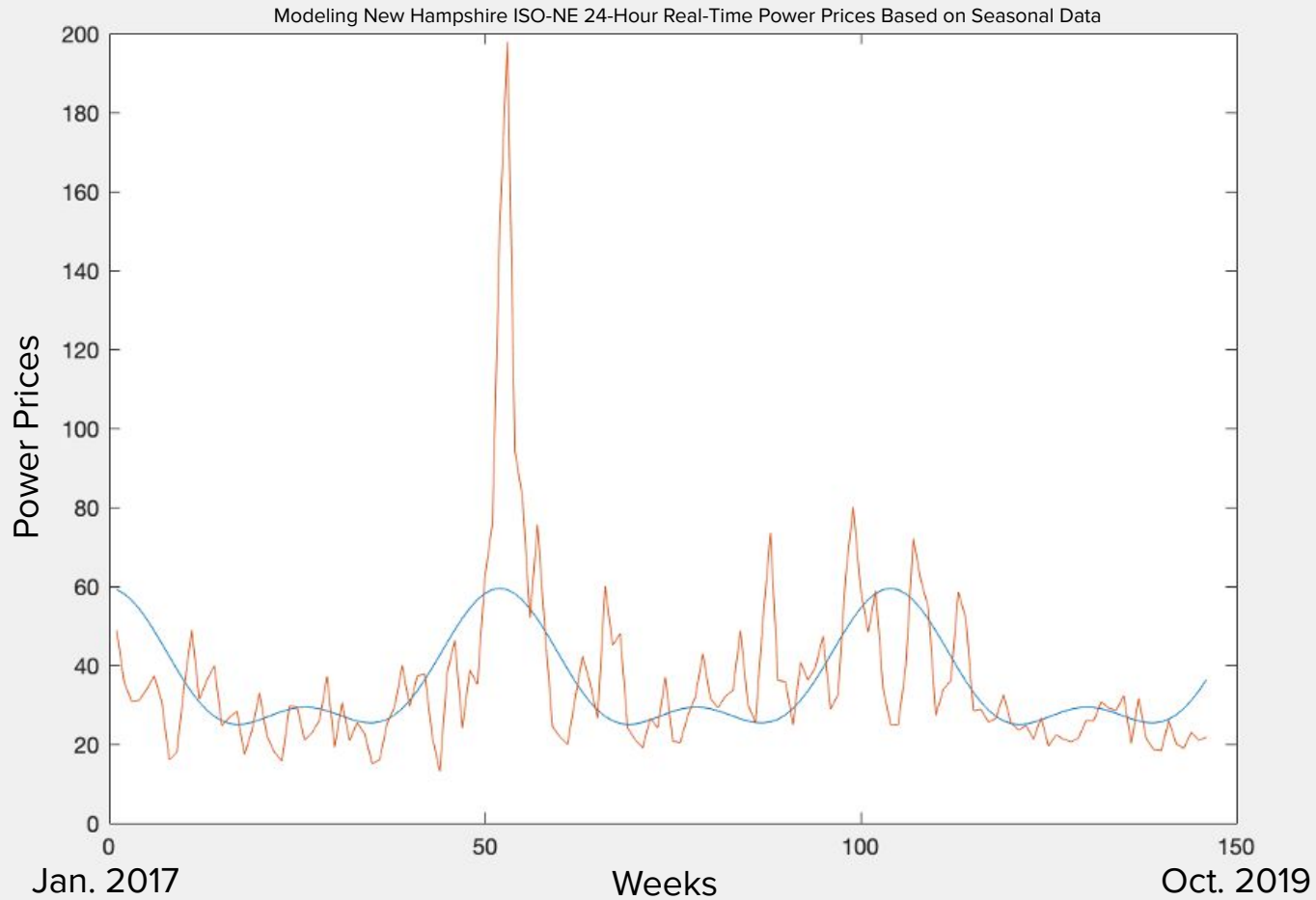
Curve Fit Found:  $y = 36.5435 - 0.1416*\sin(x) + 14.9648*\cos(x) + 1.1266*\sin(2x) + 7.7712*\cos(2x)$

# Best Fit Plot (Smoothing Curve)

Plot over the course of January 2017  
until October 2019 with a new data  
point for each week







# Data Trends and Observations

## Drastic Increase in Winter Months

- Increase may be associated with high use of heating appliances and shorter days (more lighting usages)

## Slight Increase in Summer Months

- Increase may be associated with use of air conditioning

\*graph on right only focused on the first year

