MATH 1 Homework 6

Assigned October 19th, due October 26th

- 1. (a) Use the limit definition to find the slope of the tangent line to $f(x) = x x^2$ at the point (1,0).
 - (b) Find an equation of the tangent line at the point (1,0).
 - (c) Graph both f(x) and the tangent line at the point (1,0). Be sure to label which is which.
- 2. (a) Use the limit definition to find the derivative of $f(x) = x^2 4x$.
 - (b) Check your work using the power rule.
 - (c) Graph f and f' (label which is which). Why does it make sense that f' is positive, negative, and zero for the x values that it is (when compared to the graph of f)?
- 3. (a) A particle starts by moving up along a vertical line; the graph below is of the height of the particle relative to time. When is the particle moving up? Down? Standing still?



- (b) Draw a graph of the velocity of the particle relative to time.
- (c) A second particle starts by moving up along a vertical line; the graph of its velocity relative to time is shown below. When is the particle moving up? Down? Standing still?



(d) Draw a graph of the height of the particle relative to time.

- 4. Draw a graph of a function that has the following properties on the interval [0, 1]:
 - (a) positive with positive derivative.
 - (b) negative with positive derivative.
 - (c) positive with negative derivative.
 - (d) negative with negative derivative.
- 5. Compute the following derivatives using the rules for computing derivatives. Show your work.
 - (a) g'(3) for g(x) = 3
 - (b) h'(-1) for $h(x) = 6e^x + x(x-1)$
 - (c) j'(0) for $j(x) = 3x^6 + x^2 + x 5e^x$
 - (d) k'(-2) for $k(x) = x^3 3x + 5$