

Worksheet Feb 14

1. Let  $C = C_1 + C_2$  where  $C_1$  is the semicircle  $x^2 + y^2 = 1$ ,  $y \geq 0$ , traced from  $(1, 0)$  to  $(-1, 0)$ , and  $C_2$  is the line segment from  $(-1, 0)$  to  $(1, 0)$ . Compute

$$\int_C y^2 dx + x^2 dy$$

in two ways: by direct computation and by Green's Theorem.

2. Let  $\mathbf{F}(x, y) = \langle e^{x^4} + y, x + y^2 \rangle$ .

- (a) Does  $\mathbf{F}$  satisfy the condition " $\frac{\partial Q}{\partial x} = \frac{\partial P}{\partial y}$ "?
- (b) Do  $P$  and  $Q$  have continuous first and second order partials? (You don't have to compute them. It should be clear.)
- (c) Is the domain of  $\mathbf{F}$  simply-connected?
- (d) Do you have enough information to determine whether  $\mathbf{F}$  is conservative without actually trying to find a function  $f$  such that  $\mathbf{F} = \nabla f$ ?