

Parametrization of curves

- If we are thinking of a particular particle moving around in space, the parametrization itself is important. If we only care about the points "etched out," then any parametrization will work.
- To parametrize a straight line from point a to point b , find the vector $\mathbf{d} = \mathbf{b} - \mathbf{a}$ and use the parametrization $\mathbf{r}(t) = \mathbf{a} + t\mathbf{d}, 0 \leq t \leq 1$.
- If a parametrized curve has the form $\mathbf{r}(t) = (\text{blah} \cdot \cos(t), \text{blah} \cdot \sin(t), \text{blech})$ it is a circular motion with height equal to blech and radius equal to blah , note that blah and blech may depend on t .

Differentiation

- Curves are vector functions and hence follow rules of differentiation that are essentially vector forms of the standard rules of differentiation.
- Bucky's Theorem: $|\mathbf{r}(t)|$ constant requires $\mathbf{r} \cdot \mathbf{r}' = 0$. Note that the reverse also is true.