Arc Length

- If one thinks of a curve as the path of a car driving along, the arc length is what the odometer reads.
- ullet We generally use s to stand for arc length

•
$$|\mathbf{r}'(t)| = \frac{ds}{dt}$$
.

•
$$s(T) = \int_0^T |\mathbf{r}'(t)| dt$$
.

- We often wish to reparametrize a curve in terms of s, in which case we use the following recipe:
 - find $|\mathbf{r}'(t)|$

- Calculate s(T) for an arbitrary choice of T
- Massage the answer to get T in terms of s [rather than s in terms of T.
- Since T can be any number non-negative value the above actually gives a formula for t in terms of s.
- substitute this formula into the formula for $\mathbf{r}(t)$ to get a formula $\mathbf{r}(s)$ for \mathbf{r} in terms of s.