

1. The two curves $\mathbf{r}_1(t) = \langle 2, t, t^2 - 4 \rangle$ and $\mathbf{r}_2(s) = \langle s, 3, 9 - s^2 \rangle$ both lie on a surface S and intersect at some point P .
 - (a) Find their point of intersection.
 - (b) Find the angle between the tangent vectors of the curves at the point of intersection.
 - (c) Find the equation of the tangent plane to S at the given point.

2. Does the limit

$$\lim_{(x,y) \rightarrow (1,0)} \frac{xy - y}{(x - 1)^2 + y^2}$$

exist? If so, what is its value?

3. Consider two helixes, one parametrized as $\mathbf{r}_1(t) = \langle \cos t, \sin t, t \rangle$ and the other as $\mathbf{r}_2(s) = \langle \cos s, \sin s, s^2 \rangle$. Particles move along the curves both starting out from $(1, 0, 0)$ at $s = t = 0$.

- (a) The particle on which curve starts out faster and why?
- (b) Eventually the other particle travels faster, but there is a moment when each particle has traveled exactly the same distance. Write an expression which — if solved — would reveal the time. Do not attempt to solve for the time.

4. The functions $\mathbf{r}_1(t) = \langle \cos t, \sin t, t \rangle$ and $\mathbf{r}_2(t) = \langle 1 + t, t^2, t^3 \rangle$ are parametrizations of two curves that intersect when $t = 0$.

- (a) Determine the angle of intersection between the two curves at the point of intersection.
- (b) Assuming that particles on these curves are moving with the same parameter t , is there another point in time (positive or negative) where these curves will intersect? Hint: it would help to think about the curves geometrically before making any algebraic argument.

5. Find the points on the hyperboloid $x^2 + 4y^2 - z^2 = 4$ where the tangent plane is parallel to $2x + 2y + z = 5$.

6. (30) [Multiple choice] (No partial credit) **Circle the correct answer.**

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| <ol style="list-style-type: none"> (a) A bug is crawling straight up the side of a cylinder of radius 2 feet whose equation is $x^2 + y^2 = 4$. The cylinder is rotating counterclockwise at a rate of one rotation per second. If the bug's total speed is 5π feet per second, which vector equation describes the bug's path through space? |
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- A.** $\langle 2\pi \cos(t), 2\pi \sin(t), 3\pi t \rangle$ **B.** $\langle 2\pi \cos(t), 2\pi \sin(t), 5\pi t \rangle$
- C.** $\langle 2 \cos(2\pi t), 2 \sin(2\pi t), 3\pi t \rangle$ **D.** $\langle 2 \cos(2\pi t), 2 \sin(2\pi t), 5\pi t \rangle$
- E.** $\langle 3 \cos(2\pi t), 3 \sin(2\pi t), 3\pi t \rangle$